

The Mathematical Association of Victoria
Trial Exam 2019
SPECIALIST MATHEMATICS
Written Examination 1

STUDENT NAME _____

Reading time: 15 minutes

Writing time: 1 hour

QUESTION AND ANSWER BOOK

Structure of Book

| <i>Number of questions</i> | <i>Number of questions to be answered</i> | <i>Number of marks</i> |
|----------------------------|---|------------------------|
| 9 | 9 | 40 |

- Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners, rulers,
- Students are NOT permitted to bring into the examination room: any technology (calculators or software) notes of any kind, blank sheets of paper and/or correction fluid/tape.

Materials supplied

- Question and answer book of 14 pages
- Formula sheet.
- Working space is provided throughout the book

Instructions

- Write your **name** in the space provided above on this page.
- Unless otherwise indicated, the diagrams in this book are **not** drawn to scale.
- All written responses must be in English.

Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the examination room.

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Question 6 (5 marks)

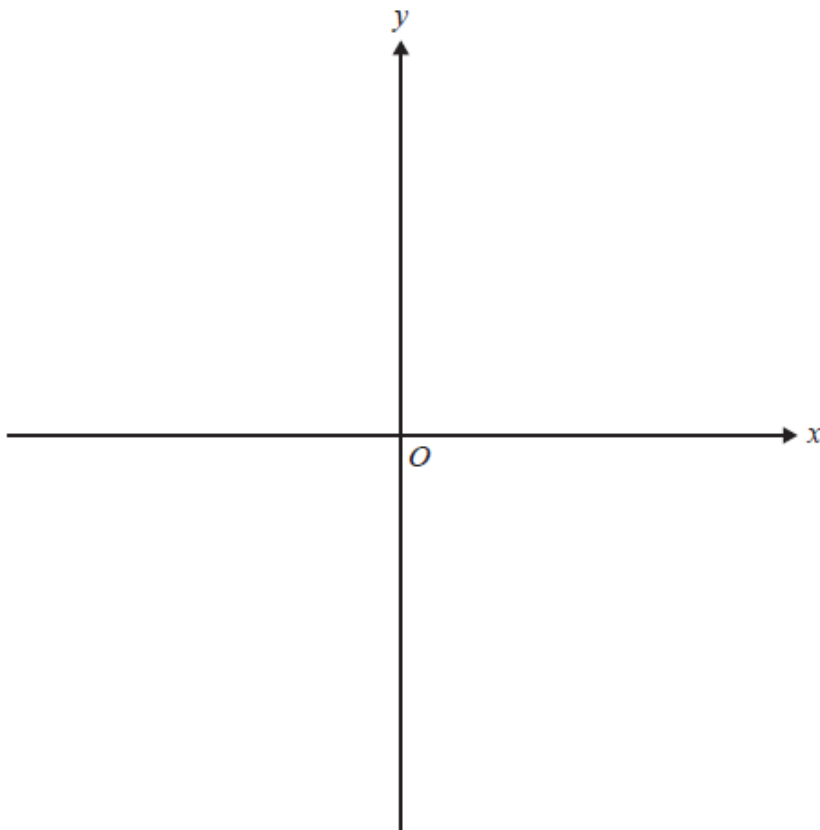
The position vector of an object moving along a curve at time t seconds is given by

$$\vec{r}(t) = (t^2 - 2t)\vec{i} + (t - 1)\vec{j}, \quad 0 \leq t \leq 2,$$

where distances are measured in metres and time is measured in seconds.

- a. Sketch the path followed by the object on the axes below, labelling all important features.

3 marks

**Working space**

Consider the function $f : D \rightarrow R$, where $f(x) = \sin^{-1}\left(\frac{2}{x-1}\right)$ and D is the maximal domain of f .

b. Determine the maximal domain D and range of f .

3 marks

c. Sketch the graph of $y = f(x)$ on the axes provided below, labelling any asymptotes with their equation and any endpoints with their coordinates.

3 marks

